

**Computer Science 411**  
**Homework 9: Turing Machines II**  
**Fall 2015**  
**Due 11/9/2015**

1. (8 points) Give a diagram for a non-deterministic Turing machine that accepts the language  $L = \{ww : w \in \{a, b\}^*\}$ . (Write this out by hand, since the Turing simulator does not allow for non-deterministic Turing machines)
2. From Hopcraft, Motwani, and Ullman. Assume that a Turing Machine has a two-way infinite tape. Somewhere on that tape is the symbol  $\$$  – either to the left or the right of the current tape head position. The rest of the tape is blank.
  - (a) (6 points) Write a Non-deterministic Turing Machine that will erase the tape. That is, write a non-deterministic Turing Machine such that there is some computational path that erases the tape and halts, and all computational paths that halt erase the tape.
  - (b) (6 points) Write a Deterministic Turing Machine that will erase the tape. That is, write a deterministic Turing machine that always halts and erases the tape.

For both parts of this question, write your solutions out by hand. (The Visual Turing software allows for neither non-determinism nor two-way infinite tapes)

3. (8 points) Using the Turing Machine software for the class, write a machine that semi-decides (that is, halts and says “yes” for all strings in the language, and runs forever for all strings not in the language) the language  $L =$  all strings over  $\{a, b, c\}$  that have more  $a$ 's than  $b$ 's and more  $b$ 's than  $c$ 's. Submit the file as <lastname>.9.tm (so I would submit it as galles.9.tm)