## Computer Science 411 <br> Homework 10: Grammars <br> Fall 2015 <br> Due 11/16/2015

1. Give an unrestricted grammar for each of the following languages:
(a) (5 points) $L=\left\{a^{n} b^{n} c^{n} d^{n}: n \geq 0\right\}$. For example, $\epsilon, a b c d$, aabbccdd, aaabbbcccddd $\in$ $L$
(b) (5 points) $L=\left\{a^{2^{n}}: n \geq 0\right\}$. For examle, a, aa, aaaa, aaaaaaaa $\in L$
2. Give a 1-counter machine for each of the following languages.
(a) (5 points) $L=$ all strings in $(a+b+c)^{*}$ that have the same number of $a \mathrm{~s}$ as $b \mathrm{~s}$. For example, $a b c, a c b b a c, b b b a a a \in L$
(b) (5 points) $L=\left\{a^{n} b^{3 n}\right\}$. For example, $a b b b, a a b b b b b b \in L$
