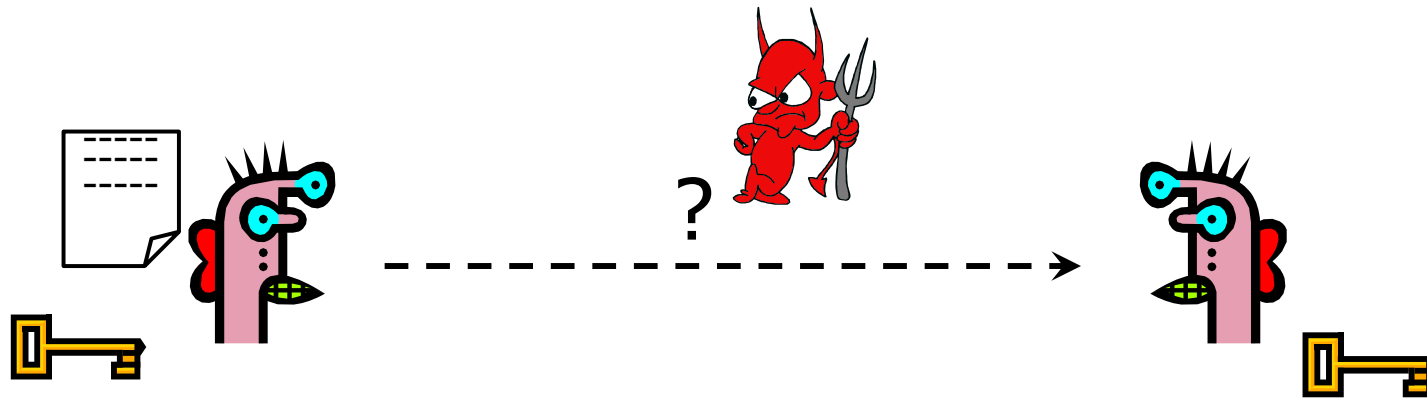


Stream Cipher

EJ Jung
ejung@cs.usfca.edu

Basic Problem



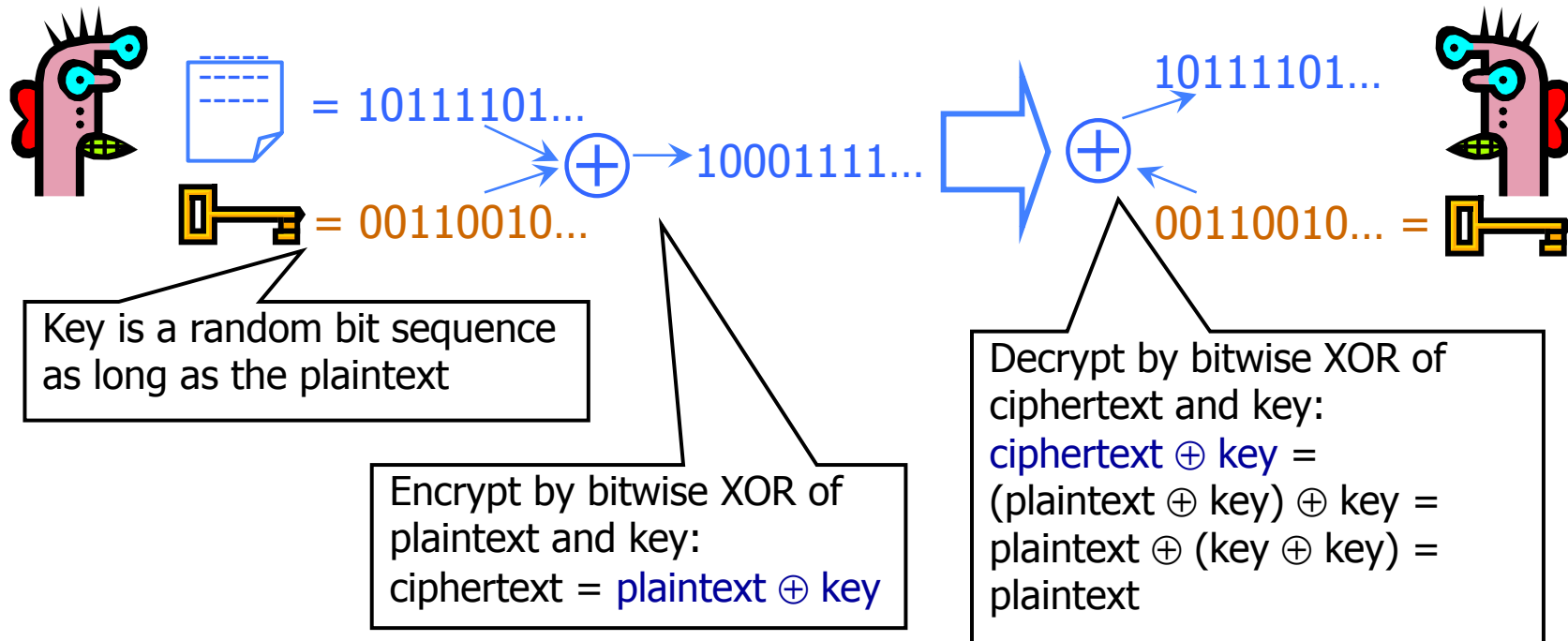
Given: both parties already know the same **secret**

Goal: send a message confidentially

How is this achieved in practice?

Any communication system that aims to guarantee confidentiality must solve this problem

One-Time Pad



Cipher achieves **perfect secrecy** if and only if there are as many possible keys as possible plaintexts, and every key is equally likely (Claude Shannon)

Advantages of One-Time Pad

➤ Easy to compute

- Encryption and decryption are the same operation
- Bitwise XOR is very cheap to compute

➤ As secure as theoretically possible

- Given a ciphertext, all plaintexts are equally likely, regardless of attacker's computational resources
- ...as long as the key sequence is truly random
 - True randomness is expensive to obtain in large quantities
- ...as long as each key is same length as plaintext
 - But how does the sender communicate the key to receiver?

Problems with One-Time Pad

- Key must be as long as plaintext
 - Impractical in most realistic scenarios
 - Still used for diplomatic and intelligence traffic
- Does not guarantee integrity
 - One-time pad only guarantees confidentiality
 - Attacker cannot recover plaintext, but can easily change it to something else
- Insecure if keys are reused
 - Attacker can obtain XOR of plaintexts

Stream Ciphers

➤ One-time pad

$\text{Ciphertext}(\text{Key}, \text{Message}) = \text{Message} \oplus \text{Key}$

- Key must be a random bit sequence as long as message

➤ Idea: replace “random” with “pseudo-random”

- Encrypt with pseudo-random number generator (PRNG)
- PRNG takes a short, truly random secret seed (key) and expands it into a long “random-looking” sequence
 - E.g., 128-bit key into a 10^6 -bit pseudo-random sequence

➤ $\text{Ciphertext}(\text{Key}, \text{Message}) = \text{Message} \oplus \text{PRNG}(\text{Key})$

- Message processed bit by bit, not in blocks

Properties of Stream Ciphers

- Usually very fast
 - Used where speed is important: WiFi, SSL, DVD
- Unlike one-time pad, stream ciphers do not provide perfect secrecy
 - Only as secure as the underlying PRNG
 - If used properly, can be as secure as block ciphers
- PRNG must be **unpredictable**
 - Given the stream of PRNG output (but not the seed!), it's hard to predict what the next bit will be
 - If $\text{PRNG}(\text{unknown seed}) = b_1 \dots b_i$, then b_{i+1} is "0" with probability $\frac{1}{2}$, "1" with probability $\frac{1}{2}$

Weaknesses of Stream Ciphers

➤ No integrity

- Associativity & commutativity: $(X \oplus Y) \oplus Z = (X \oplus Z) \oplus Y$
- $(M_1 \oplus \text{PRNG}(\text{key})) \oplus M_2 = (M_1 \oplus M_2) \oplus \text{PRNG}(\text{key})$

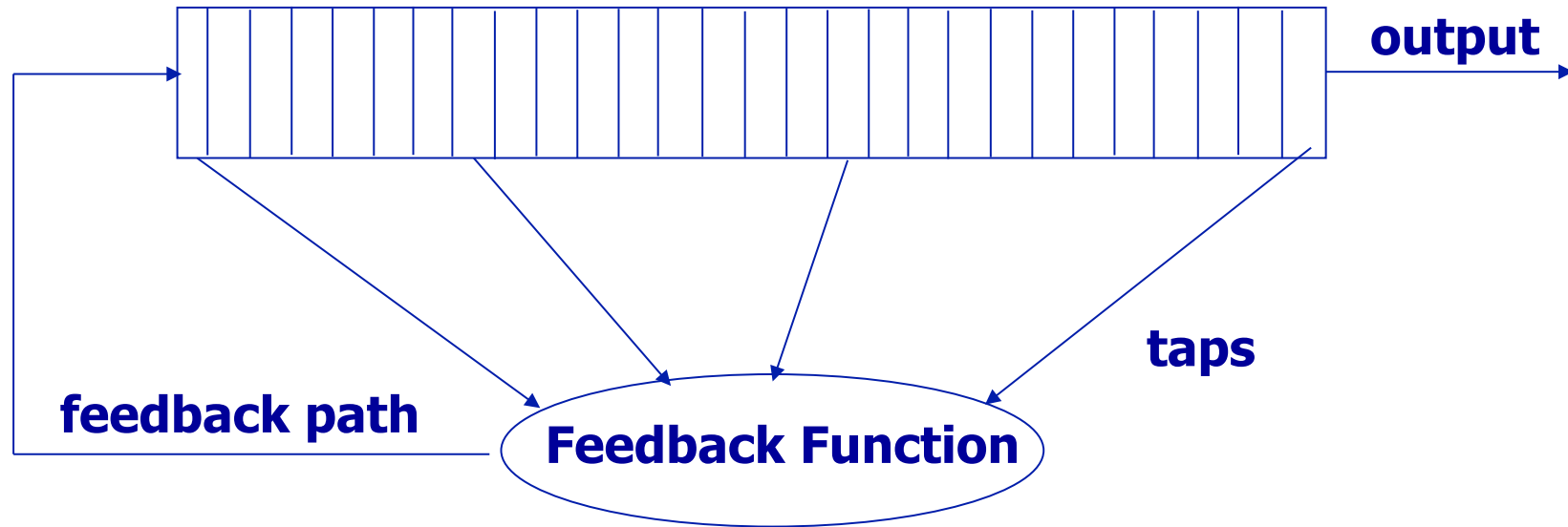
➤ Known-plaintext attack is very dangerous if keystream is ever repeated

- Self-cancellation property of XOR: $X \oplus X = 0$
- $(M_1 \oplus \text{PRNG}(\text{key})) \oplus (M_2 \oplus \text{PRNG}(\text{key})) = M_1 \oplus M_2$
- If attacker knows M_1 , then easily recovers M_2
 - Most plaintexts contain enough redundancy that knowledge of M_1 or M_2 is not even necessary to recover both from $M_1 \oplus M_2$

Stream Cipher Terminology

- Seed of pseudo-random generator often consists of **initialization vector (IV)** and **key**
 - IV is usually sent with the ciphertext
 - The key is a secret known only to the sender and the recipient, not sent with the ciphertext
- The pseudo-random bit stream produced by PRNG (IV,key) is referred to as **keystream**
- Encrypt message by XORing with keystream
 - $\text{ciphertext} = \text{message} \oplus \text{keystream}$

Generic LFSR



- The register is *seeded* with an initial value.
- At each clock tick, the feedback function is evaluated using the input from the *tapped bits*. The result is shifted into the leftmost bit of the register. The rightmost bit is shifted into the output.