## G-0: Overview

- Example games (board splitting, chess, Othello)
- Min/Max trees
- Alpha-Beta Pruning
- Evaluation Functions
- Stopping the Search
- Playing with chance

# G-1: Two player games

- Board-Splitting Game
  - Two players, V & H
  - *V* splits the board vertically, selects one half
  - *H* splits the board horizontally, selects one half
  - V tries to maximize the final value, H tries to minimize the final value

14	5	11	4
12	13	9	7
15	13	10	8
16	1	6	2

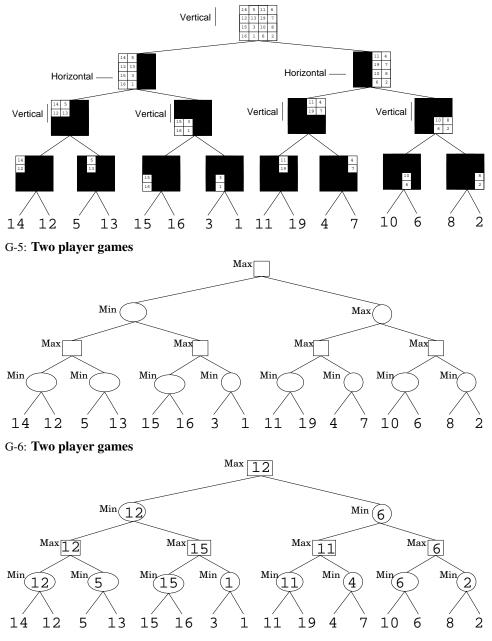
G-2: Two player games

- Board-Splitting Game
  - We assume that both players are rational (make the best possible move)
  - How can we determine who will win the game?

## G-3: Two player games

- Board-Splitting Game
  - We assume that both players are rational (make the best possible move)
  - How can we determine who will win the game?
    - Examine all possible games!

## G-4: Two player games





- Game playing agent can do this to figure out which move to make
  - Examine all possible moves
  - Examine all possible responses to each move
  - ... all the way to the last move
  - Caclulate the value of each move (assuming opponent plays perfectly)
  - •

# G-8: Two-Player Games

- Initial state
- Successor Function
  - · Just like other Searches
- Terminal Test
  - When is the game over?
- Utility Function
  - Only applies to terminal states
  - Chess: +1, 0, -1
  - Backgammon: 192 ... -192

#### G-9: Minimax Algorithm

```
Max(node)
    if terminal(node)
        return utility(node)
        maxVal = MIN_VALUE
    children = successors(node)
    for child in children
        maxVal = max(maxVal, Min(child))
    return maxVal
Min(node)
    if terminal(node)
    return utility(node)
    minVal = MAX_VALUE
    children = successors(node)
    for child in children
        minVal = min(minVal, Max(child))
    return minVal
```

#### G-10: Minimax Algorithm

• Branching factor of b, game length of d moves, what are the time and space requirements for Minimax?

#### G-11: Minimax Algorithm

- Branching factor of b, game length of d moves, what are the time and space requirements for Minimax?
  - Time:  $O(b^d)$
  - Space: O(d)
- Not managable for any real games chess has an average b of 35, can't search the entire tree
- Need to make this more managable

### G-12: > 2 Player Games

- What if there are > 2 players?
- We can use the same search tree:
  - Alternate between several players
  - Need a different evaluation function

### G-13: > 2 Player Games

- Functions return a vector of utilities
  - One value for each player