

Queues

What is a queue?

- First-in first-out data structure (FIFO)
- New objects are placed at rear
- Removal restricted to front
- Examples?

Queue ADT Operations

- **enqueue(o):** Insert o at rear of queue
 - Input: Object; Output: None
- **dequeue():** Remove object at front; error if empty
 - Input: None; Output: Object removed
- **size():** Return number of objects in queue
 - Input: None; Output: Integer
- **isEmpty():** Return a boolean indicating queue empty
 - Input: None; Output: Boolean
- **first():** Return object at front without removing; error if empty
 - Input: None; Output: Object

Example

- enqueue(5)
- enqueue(3)
- dequeue()
- enqueue(7)
- dequeue()
- front()
- dequeue()
- dequeue()
- isEmpty()
- enqueue(9)
- enqueue(7)
- size()
- enqueue(3)
- enqueue(5)
- dequeue()

Queue Interface

```
int size();  
  
bool isEmpty();  
  
Object front() throws QueueEmptyException;  
  
void enqueue(Object obj);  
  
Object dequeue() throws QueueEmptyException;
```

Underlying Representation

- Array versus Linked List
 - Pros and cons?
- Running time?
 - size
 - isEmpty
 - enqueue
 - dequeue
 - front

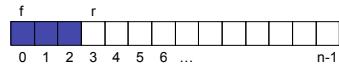
Array Implementation

enqueue(5)
enqueue(3)

Array Implementation

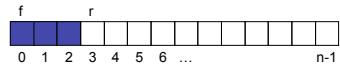
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dequeue() ?	<table border="1"> <tr><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td></tr> <tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>...</td><td></td><td>n-1</td></tr> </table>											0	1	2	3	4	5	6	...		n-1
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Circular Array



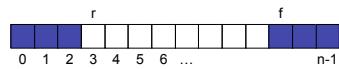
- f – stores index of cell which stores first element of queue
 - r – stores index of next available cell in queue
 - Initially, $f = r = 0$
 - How do you add a new element?
 - How do you remove an element?

Circular Array



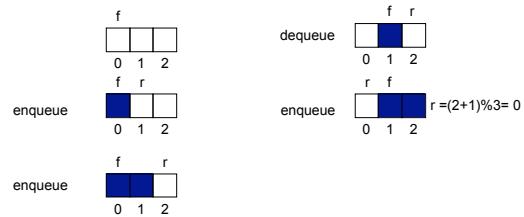
- How do you add a new element?
 - insert at array[r]
 - increment r
 - How do you remove an element?
 - return array[f]
 - increment f
 - What happens when $r \geq n-1$?

Circular Array



- Need to be able to wrap around
 - Modulo – %
 - increment f using $(f+1) \% n$
 - increment r using $(r+1) \% n$

Circular Array



Algorithms

- **size**
 - return $(N-f+r) \bmod N$
- **isEmpty**
 - return $(f == r)$
- **front**
 - if isEmpty then throw QueueEmptyException
 - return array[f]
- **dequeue**
 - if isEmpty then throw QueueEmptyException
 - temp = array[f]
 - f = $(f+1)\%N$
 - return temp
- **enqueue**
 - if size == N-1 then throw QueueFullException **SIZE MUST BE < N-1**
 - array[r] = object
 - r = $(r+1)\%N$

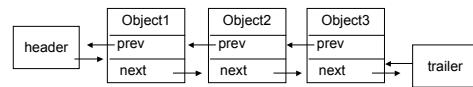
Deque

- **Double-ended queue**
 - insertFirst
 - insertLast
 - removeFirst
 - removeLast
 - first
 - last
 - size
 - isEmpty

Example

- insertFirst(3)
- insertFirst(5)
- first()
- removeFirst()
- insertLast(7)
- last()
- removeFirst()
- removeLast()

Doubly Linked List



- **Algorithms**
 - insertFirst
 - removeLast