

07-0: Binary Tree Definition

```
class Node {
  Node() { }
  Node(Comparable elem) {
    this.element = element;
  }
  Node(Object element, Node left, Node right) {
    this.element = element;
    this.left = left;
    this.right = right;
  }
  /* Access methods on next slide */
  private Node left;
  private Node right;
  private Comparable element;
}
```

07-1: Binary Tree Access Methods

```
Node left() {          void setLeft(Node left) {
  return left;          this.left = left;
}                      }

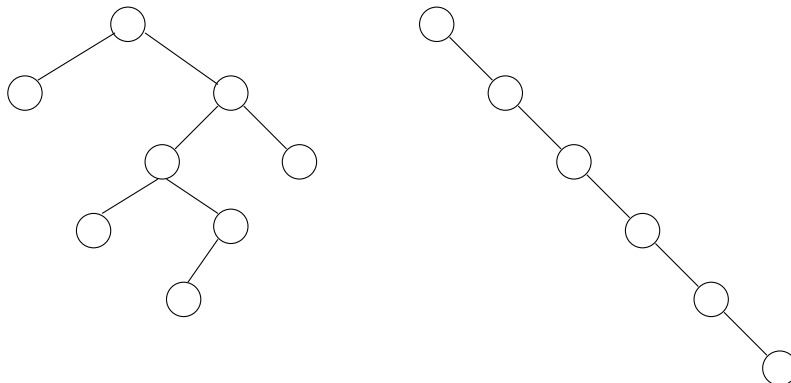
Node right() {         void setRight(Node right) {
  return right;        this.right = right;
}                      }

Comparable element() {
  return element;
}

void setElement(Comparable element) {
  this.element = element;
}
```

07-2: Tree Operations – Height

- Returns the height of the tree
 - (Length of the path to the deepest leaf) + 1



Height = 5

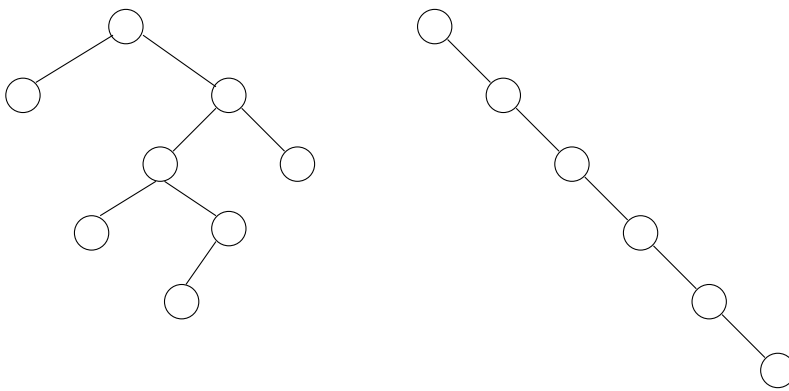
07-3: **Tree Operations – Height**

```
int height(Node tree) {
    if (tree == null)
        return 0;
    return 1 + MAX(height(tree.left()),
                   height(tree.right()));
}
```

Height = 6

07-4: **Tree Operations – NumNodes**

- Returns the number of nodes in a tree

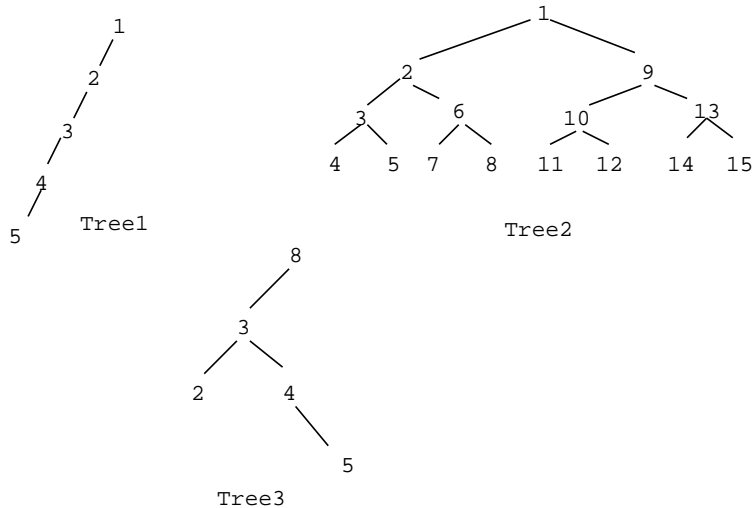


Number of Nodes = 8

Number of Nodes = 6

07-5: **Tree Operations – NumNodes**

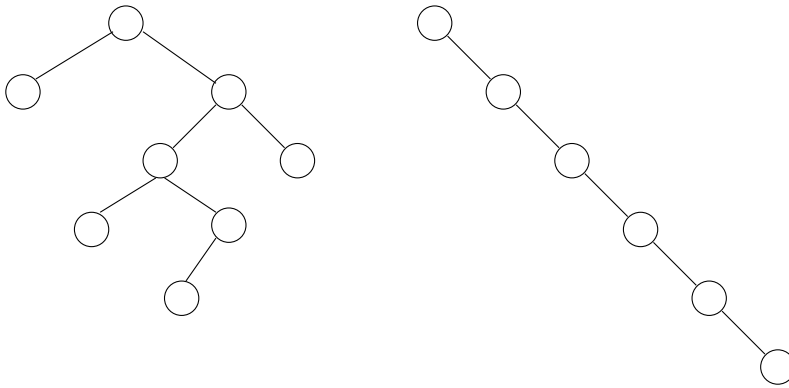
```
int numNodes(Node tree) {
    if (tree == null)
        return 0;
    return 1 + numNodes(tree.left()) +
            numNodes(tree.right());
}
```

07-6: **Writing Tree Functions**

Write `find`, `numLeaves`, `shallowestleaf`

07-7: Tree Operations – NumLeaves

- Returns the number of leaves in a tree



Number of Leaves = 4

Number of Leaves = 1

07-8: Tree Operations – NumLeaves

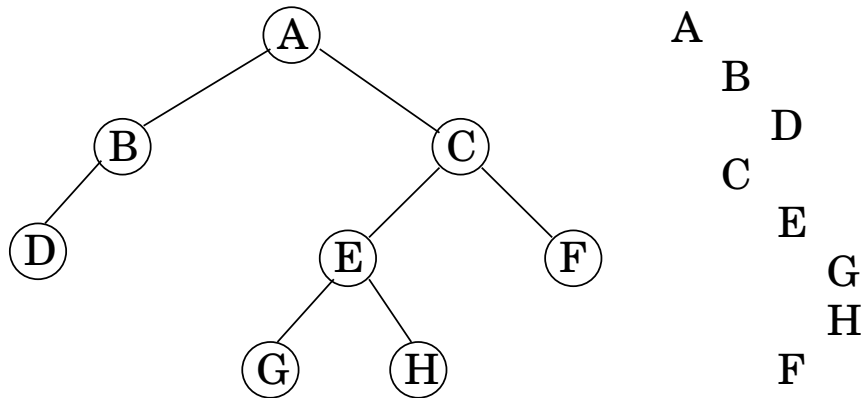
```
int numLeaves(Node tree) {
    if (tree == null)
        return 0;
    if ((tree.left() == null) &&
        (tree.right() == null))
        return 1;
    return numLeaves(tree.left()) +
           numLeaves(tree.right());
}
```

07-9: Tree Traversals

- PREORDER Traversal
 - Do operation on root of the tree
 - Traverse left subtree
 - Traverse right subtree
- INORDER Traversal
 - Traverse left subtree
 - Do operation on root of the tree
 - Traverse right subtree
- POSTORDER Traversal
 - Traverse left subtree
 - Traverse right subtree
 - Do operation on root of the tree

07-10: **PREORDER Traversal**

Printing out trees (Showing the shape of the tree in the printout)

07-11: **PREORDER Traversal**

Printing out trees (Showing the shape of the tree in the printout)

- First print the root at current indent level
 - Print the left subtree with larger indentation
 - Print the right subtree with larger indentation

07-12: **Printing Binary Trees**

```
void print(Node tree, int indent) {
    if (tree != null) {
        for(int i=0; i<indent; i++) {
            System.out.print("\t");
        }
        System.out.println(tree.element().toString());
        print(tree.left(), indent + 1);
        print(tree.right(), indent + 1);
    }
}
```

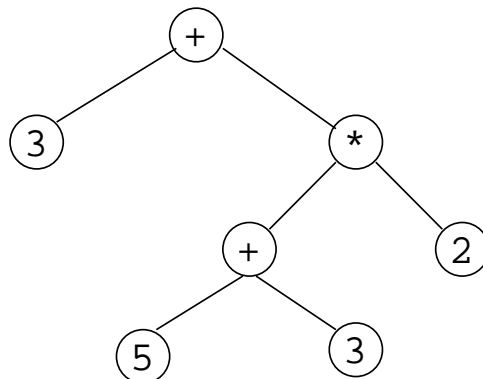
07-13: **INORDER Traversal**

Printing all elements in a Binary Search Tree in order

- (Already covered in previous slides)

07-14: **POSTORDER Traversal**

Calculating the Value of an expression tree



07-15: POSTORDER Traversal

Calculating the Value of an expression tree

- Base case:
 - Return value stored at leaf
- Recursive case:
 - Calculate value of left subtree
 - Calculate value of right subtree
 - Calculate expression value

07-16: Expression Tree Value

```
int value(Node tree) {
    if (tree.left() == null && tree.right() == null)
        return ((Integer) tree.element()).intValue();
    int left = value(tree.left());
    int right = value (tree.right());
    char op = ((Character) tree.element()).charValue();
    switch (op) {
        case '+':
            return left + right;
        case '*':
            return left * right;
        ...
    }
}
```