

**Computer Science 411**  
**Homework 11: Final Homework**  
**Fall 2013**  
**Due 12/4/2013**

1. For the language  $L =$  all strings over  $\{a, b\}$  that contain the substring  $aa$ , but not the substring  $bab$ 
  - (a) (4 points) Give either a DFA or NFA for  $L$
  - (b) (4 points) Give a regular expression for  $L$ . You can either do the mechanical conversion, or just create a regular expression yourself from scratch.
2. (8 points) Show that the language  $L =$  all strings over  $\{a, b, +, *, (, )\}$  that represent valid regular expressions over the alphabet  $\{a, b\}$  is Context-Free, but not regular
3. Show that both of the following decision problems are in **P**:
  - (a) (4 points) DNF-Satisfiability: Given a Boolean expression in *disjunctive* normal form (the disjunction of clauses, each of which is a conjunction of literals) is satisfiable.  
DNF Example: The formula  $f = (x_1 \wedge x_2) \vee (x_3 \wedge \bar{x}_4 \wedge x_5) \vee (\bar{x}_2 \wedge x_3)$  is in disjunctive normal form.
  - (b) (4 points) CNF-Tautology: Given a boolean expression in Conjunctive Normal Form, is it a tautology (that is, is it true under any truth assignment of its variables)?