

**Computer Science 411**  
**Homework 6: PDA**  
**Fall 2015**  
**Due Friday, October 16th, 2015**

1. For each of the following languages, give a push-down automaton.

(a) (4 points)  $\{a^n b^{3n} : n > 0\}$

(b) (4 points)  $\{a^n x : n \geq 0, x \in (a + b)^*, |x| = n\}$

(c) (4 points)  $L =$  all strings over  $\{a, b\}$  that do not contain the substring  $bba$

(d) (4 points)  $L =$  Valid prefix operations over the alphabet  $1, 2, 3, -, /$ . Examples:

$\in L$	$\notin L$
3	- 2 3 1
- 1 2	/ 2
- - 3 2 - 1 3	- - 3 2 - 2

2. (8 points) Give both a CFG and a PDA for the language  $L$  All strings over  $\{0, 1\}$  that are *not* of the form  $0^n 1^n$ .  $L = \overline{\{0^n 1^n : n > 0\}}$ . Thus,  $001, 100, 1001, 0110 \in L$ , while  $01, 0011, 000111 \notin L$